

OSU Name.# : \_\_\_\_\_

Lecturer: : \_\_\_\_\_

Recitation Instructor : \_\_\_\_\_

Recitation Time : \_\_\_\_\_

### INSTRUCTIONS

- **SHOW ALL WORK** in problems 2, 3, and 4 .  
Incorrect answers with work shown may receive partial credit,  
but unsubstantiated correct answers may receive NO credit.
- You don ' t have to show work in problems 1 and 5 .
- Give **EXACT** answers unless asked to do otherwise .
  - Calculators are **NOT** permitted !  
PDA ' s , laptops , and cell phones are prohibited .  
Do not have these devices out !
  - The exam duration is 55 minutes .
  - The exam consists of 5 problems starting on page 2 and ending on page 8 .  
Make sure your exam is not missing any pages before you start .

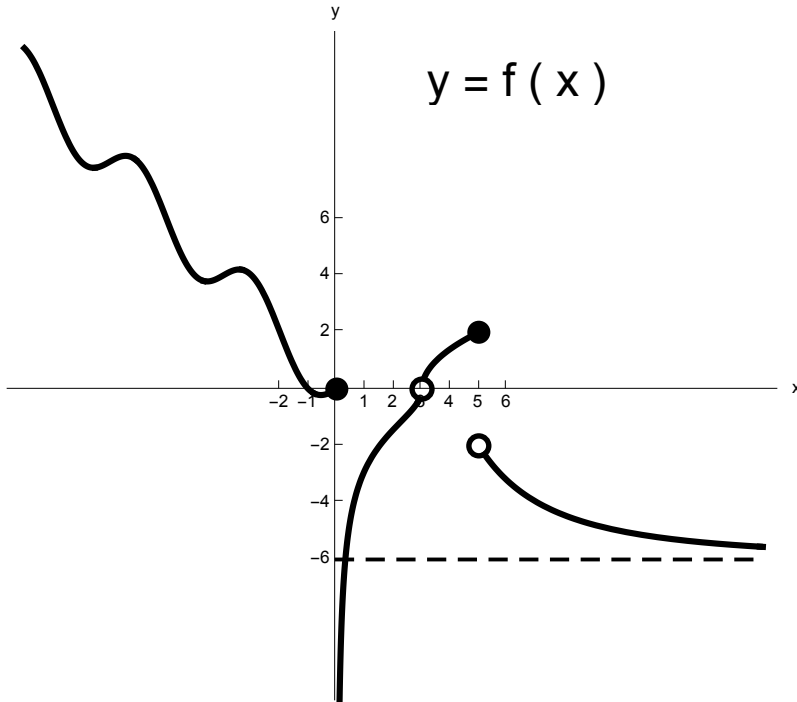
PROBLEM NUMBER	SCORE
1	( 20 )
2	( 20 )
3	( 21 )
4	( 21 )
5	( 18 )
<b>TOTAL</b>	<b>( 100 )</b>

**MIDTERM 1**  
**Form A, Page 2**

**1. (20 pts)**

The graph of a function  $f$  is given in the figure below.

Use the graph of  $f$  to answer the questions below.



(I) (1 pt) Find the domain of  $f$ .

(II) (1 pt) Find the range of  $f$ .

(III) Find the following values.

(Note: Possible answers include  $+\infty$ ,  $-\infty$ , or "does not exist".)

(a) (1 pt)  $\lim_{x \rightarrow 3} f(x) =$

(b) (1 pt)  $f(3) =$

(c) (1 pt)  $f(5) =$

**MIDTERM 1**  
**Form A, Page 3**

**1. ( CONTINUED)**

(d) (1 pt)  $\lim_{x \rightarrow 0^-} f(x) =$

(e) (1 pt)  $\lim_{x \rightarrow 0^+} f(x) =$

(f) (1 pt)  $\lim_{x \rightarrow 0} f(x) =$

(g) (1 pt)  $\lim_{x \rightarrow -\infty} f(x) =$

(h) (1 pt)  $\lim_{x \rightarrow +\infty} f(x) =$

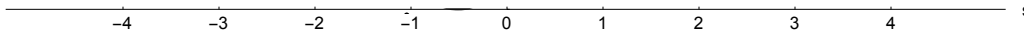
(IV) (2 pts) Find all vertical asymptotes.

(V) (2 pts) Find all horizontal asymptotes.

(VI) (6 pts) Determine the intervals of continuity for  $f$ .

**MIDTERM 1**  
**Form A, Page 4**

**2. (20 pts) SHOW YOUR WORK !**



The position,  $s(t)$ , of an object moving along a horizontal line (see the figure above) is given by

$$s(t) = t^2 - 2.$$

(I) Mark the position of the object at the time  $t = 1$  on the line above.

(II) Find the average velocity,  $v_{AV}$ , of the object during the time interval  $[1, 3]$ .

$$v_{AV} =$$

(III) Compute the average velocity,  $v_{AV}(t)$ , of the object during the time interval

(a)  $[1, t]$ , for  $t > 1$ ;

(b)  $[t, 1]$ , for  $0 < t < 1$ .

**MIDTERM 1**  
**Form A, Page 5**

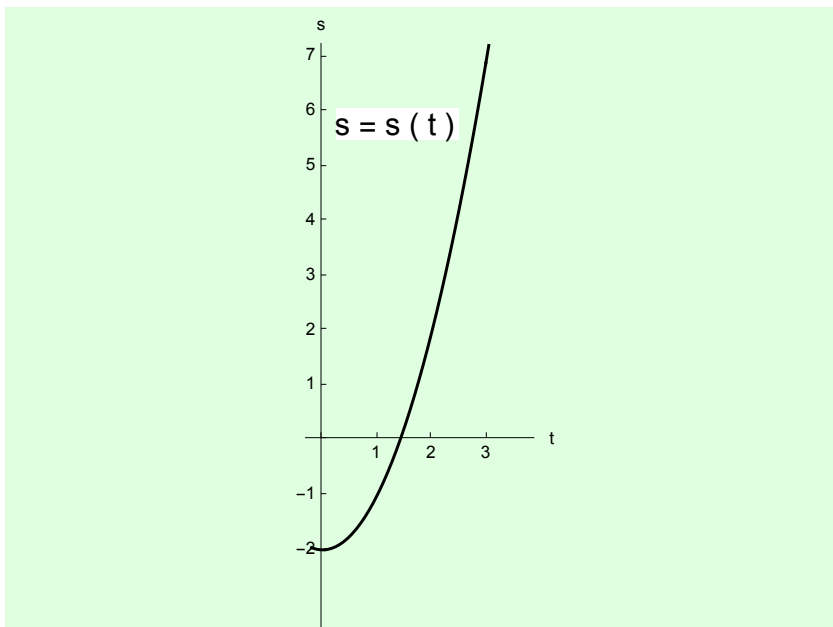
**2. (CONTINUED)**

- (IV) Find the instantaneous velocity,  $v_{inst}$ , of the object at  $t = 1$ .  
 Justify your answer.

$$v_{inst} =$$

- (V) Let  $s(t) = t^2 - 2$ .

The graph of of the function  $s$  is given in the figure below.



- (a) Assume  $P$  is a point on the graph of  $s$ . Fill in the blank.

$$P = (1, \_)$$

- (b) Plot the point  $P$  and draw the tangent line at this point in the figure above.

- (c) Find the slope,  $m_{tan}$ , of the tangent line in part (b). Explain.

$$m_{tan} =$$

**MIDTERM 1**  
**Form A, Page 6**

3. (21 pts) Evaluate the limit or say that the limit does not exist .  
If a limit does not exist, explain why. Show your work.

You may NOT use a table of values, a graph,  
or L' Hospital's Rule to justify your answer.

(Note : Possible answers include  $+\infty$  or  $-\infty$ .)

(a) (7 pts)  $\lim_{x \rightarrow 3} \frac{x^2 - 2x - 3}{\sqrt{x+1} - 2} =$

(b) (7 pts)  $\lim_{x \rightarrow 0^+} x \sin(\ln x)$

(c) (7 pts)  $\lim_{x \rightarrow 2^-} \frac{(\ln x)}{(x - 2)} =$

MIDTERM 1  
Form A, Page 7

4. (21 pts) (I) (6 pts) Determine the value of a constant  $b$  for which the function  $g$  is continuous at 0. Show your work. Justify your answer!

$$g(x) = \begin{cases} \frac{2x+b}{x-5} & \text{if } x < 0, \\ \frac{x+16}{x^2-16} & \text{if } x \geq 0, x \neq 4. \end{cases}$$

In the questions below the function  $g$  is given in part (I).

- (II) (4 pts) Evaluate the limit. Show your work!
- (a)  $\lim_{x \rightarrow -\infty} g(x) =$                       (b)  $\lim_{x \rightarrow +\infty} g(x) =$

- (III) (4 pts) Determine whether  $g$  has any horizontal asymptotes. If so, write the equation (or equations) of all horizontal asymptotes.

- (IV) (7 pts) Determine whether  $g$  has any vertical asymptotes. If so, write the equation (or equations) of all vertical asymptotes. Show your work. Justify your answer!

MIDTERM 1  
Form A, Page 8

5. (18 pts) Circle True if the statement is ALWAYS true; circle False otherwise. No explanations are required.

Let  $f$  be a one - to - one function and  $f^{-1}$  its inverse.

- (a) If the point  $(2, 5)$  lies on the graph of  $f$ , then the point  $(5, 2)$  lies on the graph of  $f^{-1}$ .  
True False

- (b)  $\sin^{-1}(\pi) = 0$  True False

If  $f$  and  $g$  are two functions defined on  $(-1, 1)$ , and if

- (c)  $\lim_{x \rightarrow 0} g(x) = 0$ , then it must be true that  
 $\lim_{x \rightarrow 0} [f(x)g(x)] = 0$ . True False

If  $f$  is continuous on  $(-1, 1)$ , and if  $f(0) = 10$  and  $\lim_{x \rightarrow 0} g(x) = 2$ ,

- (d) then  $\lim_{x \rightarrow 0} \frac{f(x)}{g(x)} = 5$ . True False

If  $f$  is continuous on  $[1, 3]$ , and if

- (e)  $f(1) = 0$  and  $f(3) = 4$ , then the equation  $f(x) = \pi$  has a solution in  $(1, 3)$ .  
True False

Let  $f$  be a positive function with vertical asymptote  $x = 5$ . Then

- (f)  $\lim_{x \rightarrow 5} f(x) = +\infty$ .  
True False