

NAME : _____

OSU Name.# : _____

Lecturer: : _____

Recitation Instructor : _____

Recitation Time : _____

INSTRUCTIONS

- **SHOW ALL WORK** in problems 1, 2, and 5 .
Incorrect answers with work shown may receive partial credit,
but unsubstantiated correct answers may receive NO credit.

You don ' t have to show work in problems 3 and 4 .

- Give EXACT answers unless asked to do otherwise .

- You do not need to simplify numerical answers such as $\frac{5}{\sqrt{8}} - \frac{3}{\sqrt{32}}$.

- Calculators are permitted EXCEPT those calculators that have computer algebra systems (CAS) or ability to communicate with others .
Furthermore, all memory must be cleared and all apps must be removed .
PDA ' s , laptops , and cell phones are prohibited .
Do not have these devices out !

- The exam duration is 55 minutes .

- The exam consists of 5 problems starting on page 2 and ending on page 8 .
Make sure your exam is not missing any pages before you start .

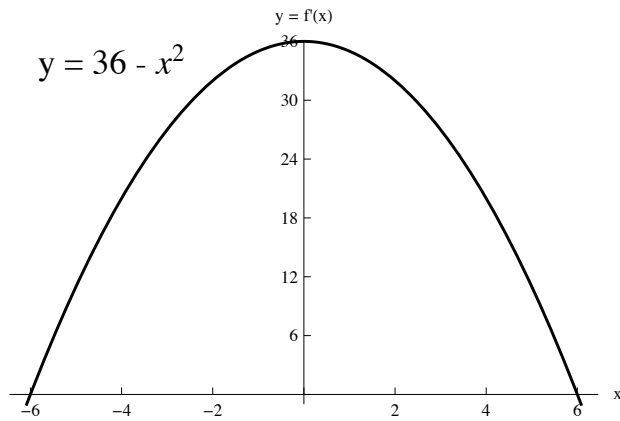
PROBLEM NUMBER	SCORE
1	(20)
2	(20)
3	(22)
4	(18)
5	(20)
TOTAL	(100)

MIDTERM 3
Form C, Page 2

1. (20 pts)

A rectangle is constructed with its base on the x - axis and two of its vertices on the parabola $y = 36 - x^2$ and above the x - axis.

(I) Make a sketch and label it.



(II) What are the dimensions of the rectangle with the maximum area?

Justify your answer !

(III) What is that maximum area?

2. (20 pts)

(I) (10 pts) Evaluate the limit. You may use L'Hospital's Rule.

$$\lim_{x \rightarrow 0^+} (1 + 3x)^{\frac{4}{x}}$$

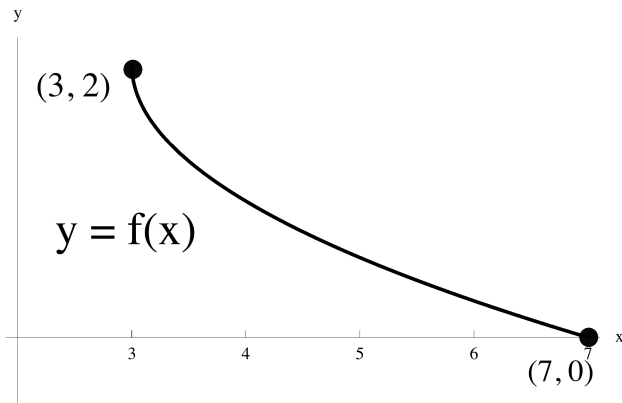
(II) (10 pts) Given the acceleration function of an object moving along a line, find the position function with the given initial velocity and position.

$$a(t) = 4t, \quad v(0) = 3, \quad s(0) = 5$$

3. (22 pts)

(I) (10 pts) EXPLANATION IS NOT REQUIRED, AND NO PARTIAL CREDIT WILL BE GIVEN.

The figure shows the graph of a function f on the interval $[3, 7]$.



(a) Find the average rate of change of the function f on the interval $[3, 7]$.

(b) Find the slope of the secant line that passes through $(3, 2)$ and $(7, 0)$.

(c) Sketch the secant line from the part (b) in the figure above.

(d) In the figure above mark the points P (if they exist) at which the slope of the tangent line equals the slope of the secant line from the part (b).

(e) Name the theorem that guarantees that such a point P exists.

(f) Sketch the tangent line at P in the figure above.

3. (CONTINUED) MULTIPLE CHOICE ! CIRCLE THE CORRECT ANSWER IN EACH PART.

(II) (3 pts)

Find the equation of the line that represents the linear approximation to the function $f(x) = e^{2x}$ at $a = 0$.

- (a) $y = 1 + 2x$; (b) $y = 1 - 2x$; (c) $y = \ln(2x + 1)$; (d) $y = x$;
(e) SUCH A LINE DOES NOT EXIST; (f) NONE OF THE PREVIOUS ANSWERS.

(III) (3 pts)

Determine the indefinite integral $\int \left(\frac{1}{1+x^2} - 3 \right) dx$.

- (a) $\ln(1+x^2) + C$; (b) $\ln(1+x^2) - 3x + C$; (c) $\tan^{-1}x - 3x + C$;
(d) $\tan^{-1}x$; (e) $\tan^{-1}x + C$; (f) NONE OF THE PREVIOUS ANSWERS.

(IV) (3 pts)

Evaluate the sum $\sum_{k=1}^3 (1+k^2)$.

- (a) 7; (b) 15; (c) 17; (d) $\frac{k(k+1)(2k+1)}{6}$;
(e) 16; (f) NONE OF THE PREVIOUS ANSWERS.

(V) (3 pts)

Given that $\int_0^6 g(x) dx = 2$, evaluate the integral $\int_0^6 (4g(x) + 1) dx$.

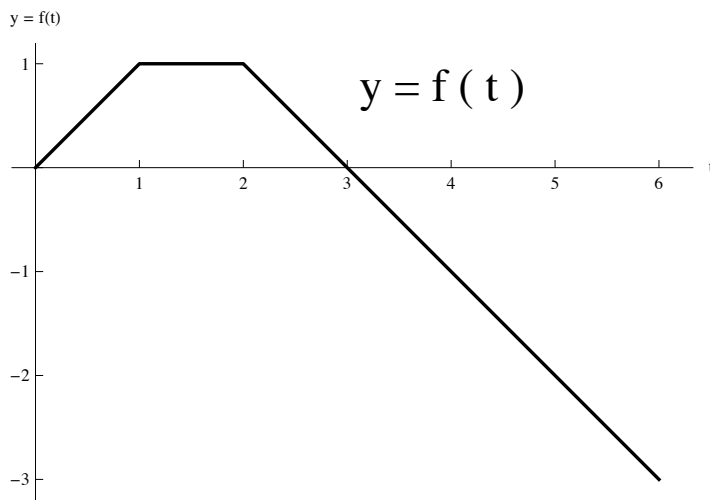
- (a) 2; (b) 8; (c) 26; (d) 54; (e) 14;
(f) NONE OF THE PREVIOUS ANSWERS.

4. (18 pts) MULTIPLE CHOICE! CIRCLE THE CORRECT ANSWER IN EACH PART.

The graph of f is shown in the figure. Let

$$A(x) = \int_0^x f(t) dt, \text{ for } 0 \leq x \leq 6, \text{ and } F(x) = \int_3^x f(t) dt, \text{ for } 3 \leq x \leq 6.$$

be two area functions for f .



(I) (3 pts) Evaluate $A(3)$.

(a) -2 ; (b) 2 ; (c) 1 ; (d) -1 ; (e) 0 ;

(f) $-\frac{3}{2}$; (g) $\frac{3}{2}$; (h) NONE OF THE PREVIOUS ANSWERS.

(II) (3 pts) Evaluate $F(3)$.

(a) 2 ; (b) 1 ; (c) 0 ; (d) $\frac{3}{2}$;

(e) $\frac{1}{2}$; (f) NONE OF THE PREVIOUS ANSWERS.

4. (18 pts) **MULTIPLE CHOICE! CIRCLE THE CORRECT ANSWER IN EACH PART.**

(III) (3 pts) Evaluate $A'(1.5)$.

- (a) 0; (b) -1; (c) 1; (d) $\frac{3}{2}$;
(e) $\frac{1}{2}$; (f) NONE OF THE PREVIOUS ANSWERS.

(IV) (3 pts) Find an expression for $F'(x)$, for $3 \leq x \leq 6$.

- (a) $F'(x) = 1$; (b) $F'(x) = 3 - x$; (c) $F'(x) = \frac{-(3-x)^2}{2}$;
(d) $F'(x) = -(3-x)^2$; (e) NONE OF THE PREVIOUS ANSWERS.

(V) (3 pts) Find an expression for $F(x)$, for $3 \leq x \leq 6$.

- (a) $F(x) = 1$; (b) $F(x) = 3 - x$; (c) $F(x) = \frac{-(3-x)^2}{2}$;
(d) $F(x) = -(3-x)^2$; (e) NONE OF THE PREVIOUS ANSWERS.

(VI) (3 pts) Evaluate $\int_0^5 |f(t)| dt$.

- (a) 0; (b) 6; (c) 4; (d) 2;
(e) 1; (f) NONE OF THE PREVIOUS ANSWERS.

5. (20 pts)

(a) Using the Fundamental theorem of calculus, evaluate the integral

$$\int_0^6 (4x - x^2) dx.$$

(b) Use the midpoint Riemann sum with $n = 3$ to approximate the value of

the integral $\int_0^6 (4x - x^2) dx.$

(c) Illustrate the midpoint Riemann sum from the part (b) by sketching the appropriate rectangles in the figure below.

