Math 1050
FINAL EXAM
December 11, 2014
Instructor's Name: $\qquad$

Circle the time your class meets:
8:00a.m. 9: $10 \quad 10: 2$
11: 30

12:40
$1: 50$
OSU email: $\qquad$ @osu.edu
Your Name $\qquad$

Signature: $\qquad$

Directions: You have 115 minutes to complete this exam. There are 35 questions. Each multiple choice question is worth 5 points, each of the other questions is worth 6 points. (There is no partial credit on multiple choice questions. Partial credit is rare but possible; so please show your work. Write your answers clearly, and use the space provided for the answer!

For problems 1-10, write the letter of the correct answer in the space provided. Only one answer is correct.

1. Subtract.
$\left(4 r^{3}+2 \mathrm{r}^{2}+6\right)-\left(-r^{2}+3 r-2\right)$
A) $5 r^{3}-r+8$
B) $5 r^{3}-r^{2}+8$
C) $4 r^{3}+3 r^{2}-3 r+4$
D) $4 r^{3}+3 r^{2}-3 r+8$
E) $4 r^{3}+3 r^{2}+3 r+4$
2. Factor: $81 y^{2}+36 y z+4 z^{2}$.
A) Nonfactorable over the integers
D) $(2 z+9 y)(2 z-9 y)$
B) $(9 y-2 z)^{2}$
E) $(9 y+2 z)(9 y-2 z)$
C) $(9 y+2 z)^{2}$
3. Write $5 \frac{7}{9} \%$ as a fraction.
A) $\frac{19}{450}$
B) $\frac{13}{25}$
C) $\frac{1}{20}$
D) $\frac{13}{225}$
E) $\frac{52}{9}$
4. Simplify: $\frac{3 n^{-4} y^{-2}}{10 n^{6} y^{9}}$.
A) $\frac{3}{10 n^{24} y^{18}}$
B) $\frac{3}{10 n^{2} y^{7}}$
C) $\frac{3}{10} n^{10} y^{11}$
D) $\frac{3}{10 n^{10} y^{11}}$
E) $\frac{3 y^{11}}{10 n^{10}}$
5. Find the coordinates of the point labeled VI.

A) $(0,2)$
B) $(2,-5)$
C) $(-1,-3)$
D) $(-4,0)$
E) $(3,5)$
6. Write the mass of Venus, which is approximately $4,870,000,000,000,000,000,000,000 \mathrm{~kg}$, in scientific notation.
A) $4.87 \times 10^{22}$
B) $4.87 \times 10^{25}$
C) $4.87 \times 10^{23}$
D) $4.87 \times 10^{26}$
E) $4.87 \times 10^{24}$
7. Multiply: $\left(x^{2}-9 x+4\right)(x-2)$.
A) $x^{3}-11 x^{2}+22 x-8$
B) $x^{3}-7 x^{2}+22 x-8$
C) $x^{3}-18 x^{2}+13 x-8$
D) $x^{3}-11 x^{2}+18 x-8$
E) $x^{3}-7 x^{2}+22 x+2$
8. Solve: $\frac{3}{7} x+5=4$.
A) $-3 \frac{1}{3}$
B) $-3 \frac{1}{6}$
C) $-2 \frac{1}{3}$
D) $-2 \frac{1}{6}$
E) $-1 \frac{1}{6}$
9. A shipping supervisor bought 36 stamps for $\$ 9.60$. The purchase included $30 \notin$ stamps and $24 \notin$ stamps. How many of each type of stamp were bought?
A) sixteen $30 \phi$ stamps; twenty $24 \not \subset$ stamps
D) twenty $30 \notin$ stamps; sixteen $24 \not \subset$ stamps
B) twenty $30 \not \subset$ stamps; fifteen $24 \not \subset$ stamps
E) twelve $30 \not \subset$ stamps; twenty-five $24 \not \subset$ stamps
C) thirteen $30 \notin$ stamps; twenty-three $24 \varnothing$ stamps
10. Factor: $25 x^{2}-9 y^{2}$.
A) $(3 y+5 x)(3 y-5 x)$
D) $(5 x+3 y)(5 x-3 y)$
B) Nonfactorable over the integers
E) $(5 x+3 y)^{2}$
C) $(5 x-3 y)^{2}$
11. Find the greatest common factor.
$4 p^{3} q^{4}, 28 p q^{3}, 36 q^{5}$
12. Solve: $6 x+7>11 x-8$.
13. Evaluate the following expression using the Order of Operations Agreement.

$$
-13^{2}+4[6 \div(6-4)]
$$

14. Ralph's Roof Repair charged $\$ 380$ for patching a damaged roof. The charge included $\$ 280$ for the replacement shingles and $\$ 20$ per hour for labor. How many hours of labor were required for the job?
15. Find the circumference of a circle with a radius of 6 cm . Use 3.14 for $\pi$.
16. Multiply: $(4 p-7)^{2}$.
17. A biker left Lewiston Wednesday morning for a 215 mile, 5 -hour trip. For the first part of the trip, the motorcycle's average speed was 40 mph . For the remainder of the trip, the average speed was 55 mph . How long did the biker ride at each speed?
18. Solve by the addition method:
$5 x-5 y=-35$
$4 x+3 y=-7$
19. Factor: $9 c^{2}+6 c x-15 c-10 x$.
20. Compute $x$.

21. The manager of a discount clothing store received two shipments of fall clothing. The cost of the first shipment, which contained 25 identical shirts and 35 identical coats, was $\$ 3125$. The second shipment, at the same prices, contained 30 of the same shirts and 25 of the same coats. The cost of the second shipment was $\$ 2900$. Find the cost of one coat.
22. The length of a rectangle is 5 in . more than twice its width. Its area is $207 \mathrm{in}^{2}$. Find the length of the rectangle.
23. Rowing with the current, a canoeist paddled 15 mi in 3 h . Against the current, the canoeist could paddle only 9 mi in the same amount of time.

Find the rate of the canoeist in calm water and the rate of the current.
24. 8 is $40 \%$ of what?
25. Simplify the following expression: $-\frac{5}{8}-\left(-\frac{2}{5}\right)+\frac{1}{2}$.
26. A tea extract that is $24 \%$ green tea is mixed with an extract that is $12 \%$ green tea.

How many gallons of the $12 \%$ green tea extract are used to make 10 gallons of an energy drink that is $18 \%$ green tea?
27. A stock analyst deposited a total of $\$ 90,000$ in two simple interest accounts. The annual simple interest rate on one account is $4 \%$. The annual simple interest rate on the second account is $13 \%$. How much was invested in each account if the total annual interest earned is $7 \%$ of the total investment?
28. Graph the solution set.

29. The price of a canoe at the Whitewater Boats Shop is $\$ 324$. This price includes the store's cost for the canoe plus a markup at the rate of $20 \%$. Find Whitewater's cost for the canoe.
30. Find the equation of the line that passes through the points $(1,2)$ and $(6,-13)$.
31. Factor: $8 y^{4}-88 y^{3}+192 y^{2}$.
32. Solve by substitution:

$$
\begin{aligned}
& y=5 x+12 \\
& y=3 x+8
\end{aligned}
$$

33. Factor: $2 c^{2}-7 c-15$.
34. Solve: $x^{2}-14 x+40=0$.
35. Divide: $\left(2 y^{2}-3 y-13\right) \div(y-4)$.

## Answer Key

1. D

Grading: (5p) No partial credit.
:

## Version B

2. C

Grading: (5p) No partial credit.
3. D

Grading: (5p) No partial credit.
4. D

Grading: (5p) No partial credit.
5. B

Grading: (5p) No partial credit.
6. E

Grading: (5p) No partial credit.
7. A

Grading: (5p) No partial credit.
8. C

Grading: (5p) No partial credit.
9. A

Grading: (5p) No partial credit.
10. D

Grading: (5p) No partial credit.
11. $\qquad$ (6p) 2 points for correct coefficient. 2 points for correct power of each variable.
12. $x<3$ (6p) 3 points for exactly one computational mistake, no points thereafter.
13. -157 (6p) 3 points for exactly one computation mistake, no points for two or more. No credit if Order of Operations is violated at any point.
14. 5 h
(6p) 3 points for correct equation; 1 point for exactly one mistake. 3 points for correct solution of proposed equation, even if equation is incorrect; 1 point for exactly one mistake. Unit (h) needs not be shown.
15. $\quad 37.68 \mathrm{~cm}$
(6p) 4 points for correct formula, but exactly one computation mistake (allow for minor rounding errors). 2 points for incorrect formula (e.g. computation of area instead, or missing the 2 ), but correct computation afterward. No points for any other situations. Unit (cm) needs not be shown.
16. $16 p^{2}-56 p+49$
(6p) 2 points for each correct term (including sign of term).
17. 4 hr at $40 \mathrm{mph} ; 1 \mathrm{hr}$ at 55 mph
(6p) 3 points for correct equation/setup. 1 point for correct solving of proposed equation, even if equation is incorrect; 1 point for each solution presented. Unit (h) needs not be shown.
18. $(-4,3)$
(6p) 4 points for exactly one computational mistake; 2 points for exactly two, no points thereafter. 2 points off if only one variable is given at the end.
19. $(3 c+2 x)(3 c-5)$
(6p) 3 points for correct grouping. 2 points for correct factorization of each group, respectively ( 1 point per group). 1 more point for correct final answer.
20.
$11^{\circ}$
(6p) 3 points for correct equation. 3 points for correct solution of proposed equation, even if equation is incorrect. Unit $\left({ }^{\circ}\right)$ needs not be shown.
21. $\$ 50.00$ (6p) 3 points for correct system of equations; 1 point for exactly one mistake, no points for two or more. 3 points for correct solution of proposed equation, even if either equation is incorrect. Take 1 points off if only the wrong variable is computed. Unit (\$) needs not be shown.
22.

23 in.
(6p) 3 points for correct equation. 3 points for correct solution of proposed equation, even if equation is incorrect. Unit (in) needs not be shown.
23. Canoeist $=4 \mathrm{mph}$; current $=1$ mph
(6p) 3 points for correct system of equations; 1 point for exactly one mistake, no points for two or more. 3 points for correct solution of proposed equation, even if either equation is incorrect. Take 2 points off if only one variable is presented at the end. Unit (mph) needs not be shown.
24.
$\lcm{20}$ $\mid(6 p) 3$ points for exactly one computational mistake, no points thereafter.
25.
$\frac{11}{40}$
(6p) 4 points for exactly one computation mistake; 2 points for exactly two; no points thereafter. Wrong addition of fractions at any point (e.g. adding denominators), no credit.
26. 5 gal
(6p) 3 points for correct equation/setup; 1 point for exactly one mistake. 3 points for correct solution of proposed setup, even if setup is incorrect; 1 point for exactly one computational mistake. Unit (lbs) needs not be shown.
27. $\$ 60,000$ at $4 \% ; \$ 30,000$ at $13 \%$
(6p) 3 points for correct equation/setup; 1 point for exactly one mistake in setup. 3 points for correct solution of proposed equation, even if equation is incorrect; 1 point for exactly one computation mistake. 1 point off if only one amount is shown. Unit (\$) needs not be shown.
28.


|  | (6p) 4 points for correct bordering line: 2 points for each correct intercept.1 <br> point for correct choice of half-plane, 1 point for bordering line being either <br> full or dotted, depending on the problem. |
| :--- | :--- |
| $\$ 270$ | (6p) 3 points for exactly one computational mistake, no points thereafter. <br> Unit (\$) needs not be shown. |

30. 

$y=-3 x+5$
(6p) 3 points for correct slope. 3 points for correct point-slope formula. Note: line equation needs not be simplified or brought to slope-intercept form.
31. $8 y^{2}(y-8)(y-3)$
(6p) 1 points for correct numeric common factor. 1 points for correct variable common factor. 4 points for correct factorization of remaining terms; 2 points if the factorization is incorrect, but the constants either add or multiply (but not both, since it is an incorrect answer) to correct, appropriate coefficients; no points for any other mistakes (e.g. one factor is actually correct, but the other is not).
32. $(-2,2)$
$(-2,2)$ (6p) 2 points for correct equation obtained by substituting first equation in the second. 2 points for correct solution of the equation, even if the equation is wrong. 2 points for computing the substituted variable. (No partial credit at any step).
33. $(c-5)(2 c+3)$
(6p) 4 points for exactly one mistake, 2 points for exactly two, no points thereafter. Guessing the coefficients is certainly allowed; if incorrect numbers are used, but at least two operations give correct answers (e.g. multiplication of initial terms and of final terms gives correct first and last term in problem's polynomial), 2 points.
34. 4,10
(6p) 2 points for correct factorization of the polynomial. 2 points for each correct solution based on the factorization obtained in step 1, even if it is incorrect.
35. $2 y+5+\frac{7}{y-4}$
(6p) 4 points for exactly one mistake, 2 points for exactly two, no points thereafter. Allow remainder be written separately (not as numerator in the fraction with divider as denominator).

