What is an Engel series?

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Abstract

We will show that any real number in the (0,1] interval has a unique expansion in what is known as an Engel series. We will discuss how this series can be used to detect the rationality of a number along with some examples. Lastly, we will discuss the ergodic properties and digit statistics of Engel series.

References

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