What is the Lambda Calculus?

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July 20, 2017

Abstract

The $\lambda$-calculus is a formal system modeling computation created by Alonzo Church, and its most prominent feature is function application via variable binding and substitution. It is equivalent to any other universal model of computation (most notably it is equivalent to the Turing machine which modern computers are based on), which means any algorithmically-solvable problem can be solved via a $\lambda$-expression. In this talk we will discuss the rules of constructing and $\lambda$-expressions and performing operations on them. We will also discuss representation of data in the $\lambda$-calculus and introduce a few special $\lambda$-expressions which perform common algorithms. Finally, we will use the $\lambda$-calculus to give a concise proof of the undecidability of the Halting problem, showing a less-traveled-by route to answering a pivotal question of the early 20th century posed by David Hilbert: the Entscheidungsproblem.

References


