

Mathematics 4530 Probability Autumn, Spring, Summer 3 credits

Catalog Description:

Combinatorial probability, random variables, independence, expectation, variance.

Purpose:

This is an introductory probability course designed to give students a firm grasp of random variables, where they occur, and how they are used, and to develop the computational tools necessary to work with them.

Prerequisite:

C- or better in 2153, 2162.xx, 2173, 2177, 2182H, 4182H; or credit for 254.xx, 263.xx, 263.01H, or 264H.

Exclusions:

Not open to students with credit for any of 530, 5530H (531H), or Stat 4201 or 420.

Follow-up Courses:

Math 3532 (actuarial science majors), Math 3589 (financial math), Stat 4202.

Text:

Probability, by Pitman, published by Springer, ISBN: 9780387979748

Topics List:

I. Discrete probability

- 1. First principles: outcome spaces, basic counting techniques, and partitions.
- 2. Venn diagrams and the inclusion-exclusion principle.
- 3. Conditional probability and independence; decision trees and Bayes' Theorem.
- 4. Discrete random variables; mass and generating functions; joint distributions.
- 5. Binomial, hypergeometric, geometric, negative binomial, and Poisson variables; applications and relationships.
- 6. Statistics on discrete variables.

II. Continuous probability

- 7. First principles: density functions, calculation of probabilities and statistics.
- 8. Moments and moment-generating functions.
- 9. Common distributions and their applications; exponential, gamma, uniform, normal.
- 10. The central limit theorem and normal approximation to the binomial distribution.
- 11. Relationships between the exponential, gamma, and Poisson distributions.
- 12. Hazard rates and survival functions.
- 13. Cumulative distribution functions, percentiles, and change of variables.
- 14. Joint distribution of continuous variables; independence and marginal distributions; density of a function of two variables

III. Statistics Material (using supplementary materials)

- 15. Chi-square distribution
- 16. t distribution
- 17. F distribution