Syllabus

Algebraic Number Theory

Instructor and Class Information

Lecturer: J. Cogdell Office: MW 632 Phone: 2-8678 Email: cogdell.1 **Course Number:**

Lecture Room: Lecture Times: 1:50 Office Hours:

About Course Goals

FORMAT

The course will meet three times a week for 55 minutes each meeting. Instructions will be mainly by lecture delivered by the instructor. It may also include occasional in-class discussion as well as short student presentations, particularly, by post-candidacy students.

DESCRIPTION & GOALS

Math 7121 is a course in algebraic number theory. The main objects of study are number fields (finite extensions of the rational number field Q); their rings of integers, prime ideals, unique factorization into prime ideals, the ideal class group, and ramification; their invariants such as the the different and discriminant, the class number and the regulator. We use a combination of local and global techniques. In particular we will study local fields, the real and complex fields, and the various p-adic fields that arise as completions of number fields, and their relation with algebraic number fields. The remaining time will be dedicated to a survey of class field theory. Class field theory centers on the following type of question: for a number field k, describe the finite abelian extensions K/k, and particularly the splitting of primes in these extensions, in terms of data internal to k.

PREREQUISITES

This section is open only to mathematics post-candidacy students and requires, in addition, the permission of the instructor.

Textbook

MAIN REFERENCE

Jim Milne: *Algebraic Number Theory*. Course notes from the University of Michigan. Available at http://www.jmilne.org/math/CourseNotes/ant.html.

ADDITIONAL REFERENCES

E. Artin: *Theory of Algebraic Numbers*, in *Exposition by Emil Artin: A Selection*, Edited by: Michael Rosen, AMS, Providence, 2006.

S. Lang, Algebraic Number Theory, (1970). Springer GTM 110.

J. Neukirch, Algebraic Number Theory (1992). Springer Grundlehren 322.

Assessments

READING, PARTICIPATION, AND ATTENDANCE

Students are required to read scheduled textbook materials and actively participate in class room discussions that arise from lecture material. Students are expected to attend all classes.

RESEARCH ORIENTED PRESENTATION

Post-candidacy students in this section are required to deliver a half hour presentation that both synthesizes lecture material and connects it to relevant research questions, more advanced theoretical topics, or applications in other fields of mathematics. The topic and required independent reading will be determined by the instructor individually in negotiation with the student. Presentations may also be replaced by respective research papers upon the request of the student.

Grading

COURSE GRADE

The grades for this course section are "satisfactory" (S) or "unsatisfactory" (U). A satisfactory outcome requires continued active participation in class (weighed about 20%) and is further based on the student's performance during the presentation (weighed about 80%).

Weekly Schedule

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Week 1	Integrality, rings of integers in a number field
Week 2	The trace form; discriminants of number fields
Week 3	Dedekind domains; localization
Week 4	Prime factorization of ideals; fractional ideals
Week 5	Factorizations in extensions
Week 6	The discriminant and different
Week 7	Finiteness of the class number
Week 8	Class number & Minkowski's geometry of numbers
Week 9	Dirichlet unit theorem; the regulator
Week 10	Cyclotomic fields
Week 11	Valuations; local fields
Week 12	Hensel's Lemma & Krasner's Lemma
Week 13	Ramified and unramified extensions of local fields
Week 14	Class field theory

General Policies

ACADEMIC MISCONDUCT

It is the responsibility of the Committee on Academic Misconduct to investigate or establish procedures for the investigation of all reported cases of student academic misconduct. The term "academic misconduct" includes all forms of student academic misconduct wherever committed;

illustrated by, but not limited to, cases of plagiarism and dishonest practices in connection with examinations. Instructors shall report all instances of alleged academic misconduct to the committee (Faculty Rule 3335-5-487). For additional information, see the Code of Student Conduct (http://studentaffairs.osu.edu/info_for_students/csc.asp)."

DISABILITY SERVICES

Students with disabilities that have been certified by the Office for Disability Services will be appropriately accommodated and should inform the instructor as soon as possible of their needs. The Office for Disability Services is located in 150 Pomerene Hall, 1760 Neil Avenue; telephone 292-3307, TDD 292-0901; http://www.ods.ohio-state.edu/.